

Exercise I

$$1 \rightarrow E = \phi + KE_{\max}$$

$$\frac{hc}{\lambda} = \frac{hc}{\lambda_0} + KE_{\max}$$

$hc = 1242 \text{ eV}\cdot\text{nm}$

$KE_{\max} = 1.5 \text{ eV}$

$\lambda_0 = 230 \text{ nm}$

?

$$\Rightarrow \boxed{\lambda = 180 \text{ nm}}$$

2 > for perfect absorption & a parallel beam
→ Radiation force = $\frac{I}{c}$ x projected area



$$= \frac{I}{c} \times \pi R^2$$

3 > Similar to previous one

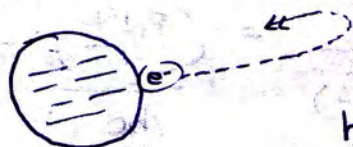


$$\text{Radiation force} = \frac{I}{c} \times \frac{1}{2} \pi \cdot 2R$$
$$= \frac{I}{c} \pi R$$

4 > The potential acquired by the sphere will be the stopping potential because once it acquires that potential, the photoelectrons ejected from it are not able to escape to infinity and hence fall back to it

$$E = \phi + KE_{\max}$$

$$\frac{hc}{\lambda} = \phi + eV_s$$



$$hc = 1242 \text{ eV}\cdot\text{nm}$$

$$\lambda = 200 \text{ nm}$$

$$\phi = 2 \text{ eV}$$

$$\Rightarrow \boxed{V_s = 4.21 \text{ V}}$$

5> "d" is the incorrect statement
 Since X ray photons have lower wavelength than visible photons, hence they are more energetic

6> ∴ $\lambda_{\text{debroglie}} = \frac{h}{p}$

⇒ The 3 particles have same momentum

also $K = \frac{1}{2}mv^2 = \frac{p^2}{2m}$

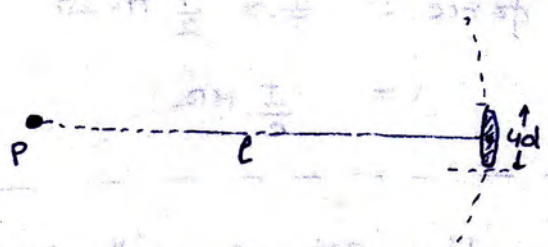
⇒ $K \propto \frac{1}{m}$

⇒ ∴ $m_e < m_p < m_d$

⇒ $K_e > K_p > K_d$

⇒ $E_1 > E_3 > E_2$

7>



Energy received = (Intensity × Area) × time

= $\frac{P}{4\pi r^2} \times 4\pi d^2 \times t$

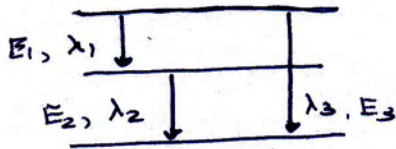
= $\frac{P d^2 t}{r^2}$

no. of photons received =

$\frac{E}{\left(\frac{hc}{\lambda}\right)} = \frac{\left(\frac{P d^2 t}{r^2}\right)}{\left(\frac{hc}{\lambda}\right)} = \frac{P \lambda d^2 t}{h c r^2}$

VIRUP

8 >



$$E_3 = E_1 + E_2$$

$$\Rightarrow \frac{hc}{\lambda_3} = \frac{hc}{\lambda_1} + \frac{hc}{\lambda_2}$$

$$\Rightarrow \boxed{\lambda_3 = \frac{\lambda_1 \lambda_2}{\lambda_1 + \lambda_2}}$$

9 >

$$r = \frac{mv}{qB}$$

$$mvr = \frac{nh}{2\pi}$$

$$\Rightarrow \cancel{m} \left(\frac{qBr}{m} \right) r = \frac{nh}{2\pi}$$

$$r = \sqrt{\frac{nh}{2\pi eB}}$$

$$r_{\min} = \sqrt{\frac{h}{2\pi eB}}$$

10 >

$$\frac{1}{\lambda} = R \left(1 - \frac{1}{n^2} \right)$$

$$\frac{1}{\lambda R} = 1 - \frac{1}{n^2}$$

$$\Rightarrow \frac{1}{n^2} = 1 - \frac{1}{\lambda R}$$

$$\Rightarrow n^2 = \frac{\lambda R}{\lambda R - 1} \Rightarrow n = \sqrt{\frac{\lambda R}{\lambda R - 1}}$$

11 > Shortest wavelength of Lyman

$$\frac{1}{\lambda} = R \left(\frac{1}{1^2} - \frac{1}{\infty^2} \right)$$

$$\Rightarrow \boxed{\frac{1}{\lambda} = R}$$

$$\Rightarrow \boxed{\lambda = \frac{1}{R}}$$

1st member of Balmer series

$$\frac{1}{\lambda} = R \left(\frac{1}{2^2} - \frac{1}{3^2} \right)$$

$$\frac{1}{\lambda} = R \cdot \frac{5}{36}$$

$$y = \frac{36}{5R}$$

$$\Rightarrow \boxed{y = \frac{36}{5} > \lambda}$$

$$\begin{aligned}
 12 > \lambda_{\text{eff}} &= \lambda_1 + \lambda_2 \\
 &= \frac{1}{T_{\text{mean}_1}} + \frac{1}{T_{\text{mean}_2}} \\
 &= \frac{1}{1620} + \frac{1}{405}
 \end{aligned}$$

for decay of $3/4$ sample $\Rightarrow T = 2 \times T_{\text{half}}$

$$= 2 \times \frac{\ln 2}{\lambda_{\text{eff}}}$$

$$= 2 \times \frac{\ln 2}{\frac{1}{1620} + \frac{1}{405}}$$

$$= 449 \text{ years}$$

13 > Temperature has No effect

14 > after 2 half lives the sample is $1/4$ th of original sample \Rightarrow activity becomes $1/4$ th of original activity

15 > Probability of survival = $p = e^{-\lambda t}$

$$= e^{-\lambda \times 2 \cdot t_{1/2}}$$

$$= e^{-\lambda \times 2 \times \frac{\ln 2}{\lambda}}$$

$$= e^{-\ln 4}$$

$$= \frac{1}{4}$$

\Rightarrow Probability of disintegration = $\frac{3}{4}$

$$16 > \text{Power} = v i = (100 \times 10^3) \times (10 \times 10^{-3})$$

0.2% Energy \rightarrow x ray

\Rightarrow 99.8% Energy \rightarrow heat

$$\begin{aligned} \Rightarrow \text{Rate of heating} &= \frac{99.8}{100} (\text{Power}) \\ &= \frac{99.8}{100} \times 1000 \text{ Joules/sec} \\ &= \frac{99.8}{100} \times \frac{1000}{4.18} \text{ (cal/sec)} \\ &= 238.75 \text{ (cal/sec)} \end{aligned}$$

$$17 > \sqrt{f} = a(z-1)$$

$$\sqrt{f} = \sqrt{\frac{3RC}{4}} (z-1)$$

$$f = \frac{3RC}{4} (z-1)^2$$

$$\frac{c}{\lambda} = \frac{3RC}{4} (z-1)^2$$

$$\Rightarrow z = 1 + \sqrt{\frac{4}{3R}} \rightarrow 1.785 \times 10^{-10} \rightarrow 1.09 \times 10^7$$

$$\Rightarrow \boxed{z = 27}$$

18 > high thermal conductivity to ensure that the heat is easily dissipated and high atomic No. ensures efficiency of x-ray production

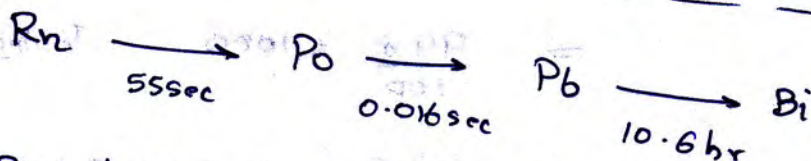
$$19 > \quad \sqrt{f} = a(31-1)$$

$$\sqrt{f'} = a(51-1)$$

$$\frac{f'}{f} = \left(\frac{5}{3}\right)^2$$

$$\Rightarrow \boxed{f' = \frac{25}{9} f}$$

20 >



\therefore Rn has half life of 55 seconds, most of it would be converted to Po in 5 mins and even Po would have converted to Pb since the half life is very very small but the lead ~~is~~ ~~not~~ would be mostly intact because of high half life \Rightarrow greatest mass \rightarrow Lead

$$n = \frac{\text{Power}}{\text{Energy of Each photon}}$$

$$\Rightarrow n \propto \frac{1}{E_0}$$

$$\therefore E_{0\text{blue}} > E_{0\text{red}}$$

~~$n_{\text{blue}} > n_{\text{red}}$~~

$$n_{\text{blue}} < n_{\text{red}}$$

Q25

$$\frac{hc}{\lambda} = \phi + K$$

$$\frac{hc}{\left(\frac{3\lambda}{4}\right)} = \phi + K'$$

$$\Rightarrow \frac{4}{3} \left(\frac{hc}{\lambda} \right) = \phi + K'$$

$$\Rightarrow \frac{4}{3} (\phi + K) = \phi + K'$$

$$\Rightarrow \boxed{K' = \frac{\phi}{3} + \frac{4K}{3}}$$

$$\Rightarrow K' > \frac{4K}{3}$$

Q26

$$h\nu = \phi + eV_s$$

$$2h\nu = \phi + eV_s'$$

$$\Rightarrow 2(\phi + eV_s) = \phi + eV_s'$$

$$\Rightarrow \phi + 2eV_s = eV_s'$$

$$\Rightarrow \boxed{V_s' = 2V_s + \frac{\phi}{e}}$$

Q27

$$K = \frac{p^2}{2m} \Rightarrow p = \sqrt{2mK}$$

$$\lambda = \frac{h}{p} = \frac{h}{\sqrt{2mK}}$$

$$K = K_0 + eV$$

$$= 100 \text{ eV} + e \times 50 \text{ V}$$

$$= 150 \text{ eV}$$

$$= 6.63 \times 10^{-34}$$

$$\sqrt{2 \times 9.1 \times 10^{-31} \times 150 \times 1.6 \times 10^{-19}}$$

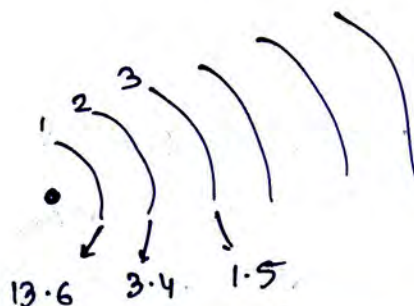
$$= 1 \text{ \AA}$$

Q28: $\lambda = \frac{h}{p} \Rightarrow p = \frac{h}{\lambda} = \frac{h}{0.1 \times 10^{-10}}$

$\Rightarrow p = 10^{12} h$

Q29: $E = \phi + eV_s$
 $= 1.7 \text{ eV} + e \times 10.4$
 $= 12.1 \text{ eV}$

So 12.1 is obtained
 by jump from 3 \rightarrow 1



Q30: A photon is either absorbed by an electron or it is not. ~~or~~ And if absorbed, it is completely absorbed. So one photon can eject only one electron

Q31
$$\frac{N_1 = N_0 e^{-10\lambda_0 t}}{N_2 = N_0 e^{-\lambda_0 t}}$$

$\left(\frac{N_1}{N_2}\right) = e^{-9\lambda_0 t}$
 $\rightarrow 1/e$

$\Rightarrow e^{-1} = e^{-9\lambda_0 t}$

$\Rightarrow 9\lambda_0 t = 1 \Rightarrow t = \frac{1}{9\lambda_0}$

Q32: ~~Because~~ If the total energy falling is increased and simultaneously the energy of each photon is also increased \rightarrow That means that total number of photons falling on the metal remains the same \Rightarrow No increase in current

Q33

$$N = N_0 e^{-\lambda t}$$

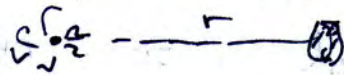
$$\frac{N}{N_0} = e^{-\lambda \left(\frac{t}{\lambda}\right)}$$

$$\Rightarrow \frac{N}{N_0} = \frac{1}{e}$$

Q34 \therefore increasing the distance only changes the intensity and has no effect on frequency, it has no effect on stopping potential

Q35: $\therefore i \propto I$
 \downarrow
 intensity

$$I = \frac{P}{4\pi r^2}$$



$$\Rightarrow \boxed{i \propto \frac{1}{r^2}} \text{ hence "D"}$$

$$Q36 \quad \neq \frac{hc}{\lambda_1} = \phi + K_1$$

$$\frac{hc}{\lambda_2} = \phi + K_2$$

$$\Rightarrow \frac{\lambda_1}{\lambda_2} = \frac{\phi + K_2}{\phi + K_1}$$

$$\Rightarrow 2\phi + 2K_1 = \phi + K_2$$

$$\Rightarrow \boxed{K_2 = 2K_1 + \phi}$$

Q37

$$hf = \phi + eV$$

$$\Rightarrow \cancel{V =}$$

$$hf_0 = \phi + e \times 0$$

$$\Rightarrow \boxed{\phi = hf_0}$$

$$hf_1 = \phi + KEmax$$

$$hf_1 = hf_0 + KEmax$$

$$\Rightarrow \boxed{KEmax = h(f_1 - f_0)}$$

Q38

$$E = \phi + KEmax$$

$$E - \phi = \frac{1}{2}mv^2$$

$$\Rightarrow v = \sqrt{\frac{2(E - \phi)}{m}}$$

$$\frac{v_1}{v_2} = \sqrt{\frac{E_1 - \phi}{E_2 - \phi}}$$

$$\frac{v_1}{v_2} = \sqrt{\frac{2\phi - \phi}{5\phi - \phi}}$$

$$\boxed{\frac{v_1}{v_2} = \frac{1}{2}}$$

$$Q39 \quad \frac{hc}{\lambda} = \phi + eV$$

$$\frac{hc}{\lambda} - \phi = eV$$

$\therefore v_1, v_2, v_3$ are in AP

$$\Rightarrow v_2 - v_1 = v_3 - v_2$$

$$\Rightarrow \left(\frac{hc}{\lambda_2} - \phi\right) - \left(\frac{hc}{\lambda_1} - \phi\right) = \left(\frac{hc}{\lambda_3} - \phi\right) - \left(\frac{hc}{\lambda_2} - \phi\right)$$

$$\Rightarrow \frac{1}{\lambda_2} - \frac{1}{\lambda_1} = \frac{1}{\lambda_3} - \frac{1}{\lambda_2}$$

$$\Rightarrow hP$$

Q40

$$E = \phi + KE_{max}$$

$$5\text{eV} = \phi + 2\text{eV}$$

$$\Rightarrow \phi = 3\text{eV}$$

$$\Rightarrow E' = \phi + eVs$$

$$\Rightarrow 6\text{eV} = 3\text{eV} + eVs$$

$$\Rightarrow V_s = 3\text{V} \quad \boxed{V_s = 3\text{V}}$$

\Rightarrow Anode voltage must be -3V w.r.t cathode

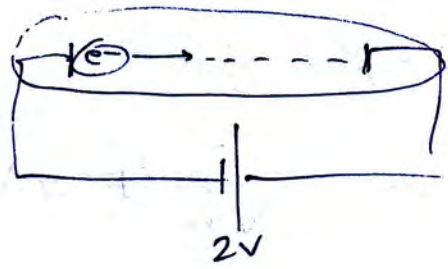
Q41:

$$E = \phi + KE_{max}$$

$$\frac{hc}{\lambda} = \phi + KE_{max}$$

$\lambda = 200\text{nm}$ 4.5eV

$$\Rightarrow KE_{max} = 1.7\text{eV}$$



$$0 \leq KE \leq 1.7\text{eV}$$

$$KE \text{ at collection} = KE + eV$$
$$= KE + e \times 2\text{V}$$

$$\Rightarrow \boxed{2 \leq KE \text{ at collection} \leq 3.7\text{eV}}$$

On reversing the polarity, no electron will reach anode

Q42: Only photocurrent (i.e. no of electrons emitted) is affected

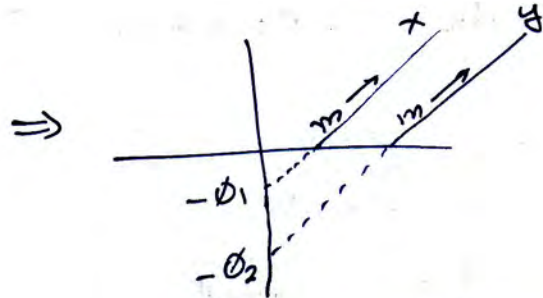
Q43

$$hf = \phi + eV$$

$$\Rightarrow V = \left(\frac{h}{e}\right) f - \phi$$



$$\Rightarrow \boxed{y = mx - \phi}$$



Q44

Since the intensity is constant & energy of each photon is increased, the no. of photons decreases

\Rightarrow Current decreases

Q45

$$\frac{1}{4\pi\epsilon_0} \frac{q \cdot 3q}{r^2} = \frac{mv^2}{r}$$

$$\Rightarrow r = \frac{3q^2}{4\pi\epsilon_0 m v^2}$$

also $mvr = \frac{nh}{2\pi}$

$$m \cdot \frac{3q^2}{4\pi\epsilon_0 m v^2} = \frac{nh}{2\pi}$$

\Rightarrow for nearest : $n = 1$

$$\Rightarrow \boxed{v = \frac{3q^2}{2\epsilon_0 h}}$$

46 > $mvr = \frac{nh}{2\pi}$

$\Rightarrow \boxed{J_n = \text{const} \times n}$

$v = \frac{zc^2}{2\pi n h}$

$\Rightarrow \boxed{v = \frac{\text{const}}{n}}$

$\lambda_n = \frac{h}{p}$

$\Rightarrow \lambda_n = \frac{h}{mv}$

$\Rightarrow \boxed{\lambda_n = \frac{\text{const}}{v}}$

$\Rightarrow \boxed{\lambda_n = \text{const} \times n}$

$\Rightarrow \boxed{\lambda_n \propto J_n}$

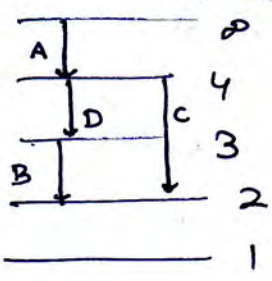
47 > $L = \frac{3h}{2\pi} \Rightarrow 3^{\text{rd}} \text{ orbit}$

$E_{3^{\text{rd}}} = -1.5 \text{ eV} \quad \& \quad KE = -E$

$\Rightarrow KE = 1.5 \text{ eV}$

~~48 > A \rightarrow longest \therefore shortest energy gap
 C \rightarrow shortest \therefore longest energy gap~~

48 > D \rightarrow longest wavelength
 \therefore smallest gap of energy
 C \rightarrow shortest wavelength
 \therefore Biggest energy gap



49 >

$$f = \frac{v}{2\pi r}$$

$$= \frac{m z^2 e^4}{4\epsilon_0^2 n^3 h^3}$$

$$= \left(\frac{m z^2 e^4}{8\epsilon_0^2 n^2 h^2} \right) \frac{2}{nh}$$

$$= \frac{2E_n}{nh}$$

$$v = \frac{z c^2}{2\epsilon_0 n h}$$

$$r = \frac{\epsilon_0 n^2 h^2}{\pi m z e^2}$$

50 > E Ionization Energy = $2.18 \times 10^{-18} \text{ J}$

Energy in 3rd orbit = $\frac{1}{9}$ th of Energy of 1st orbit

\Rightarrow Ionization from that level, Energy required

$$= \frac{1}{9} \times 2.18 \times 10^{-18} \text{ J}$$

$$= 2.42 \times 10^{-19} \text{ J}$$

$$51 > E_{4n} - E_{2n} = -13.6 z^2 \left(\frac{1}{(4n)^2} - \frac{1}{(2n)^2} \right)$$

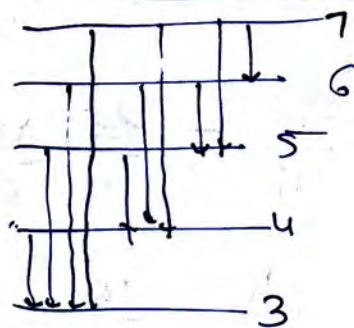
$$E_{2n} - E_n = -13.6 z^2 \left(\frac{1}{(2n)^2} - \frac{1}{n^2} \right)$$

Taking ratio : $z^0 n^0$

52 > 2nd excited state $\Rightarrow n=3$

So $n=7$

\Rightarrow 6th excited state



$$537 \quad r = 0.53 \frac{n^2}{Z} \text{ \AA}$$

$$\Rightarrow r \propto n^2$$

$$\Rightarrow (n+1)^2 - n^2 = (n-1)^2$$

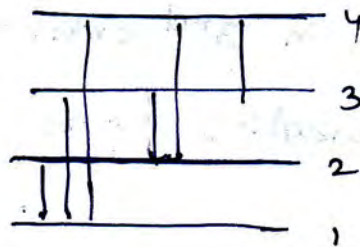
$$\cancel{n^2} + 1 + 2n - \cancel{n^2} = n^2 + 1 - \cancel{2n}$$

$$\Rightarrow \boxed{n=4}$$

54) 6 different wavelengths

$$\Rightarrow n_2 = 4$$

So if Energy of emitted photon can be greater, less or equal to absorbed photon n_1 can only be 2



$$55) \quad M \rightarrow L \Rightarrow 3 \rightarrow 2$$

$$r \propto n^2$$

$$\Rightarrow \boxed{\frac{r_f}{r_i} = \frac{4}{9}}$$

$$\frac{kze^2}{r^2} = m\alpha c$$

$$\Rightarrow \alpha c \propto \frac{1}{r^2}$$

$$\Rightarrow \frac{Q_f}{Q_i} = \frac{\cancel{36}}{\cancel{16}} \frac{81}{16}$$

$$\Rightarrow \boxed{\frac{Q_i}{Q_f} = \frac{16}{81}}$$

$$Q56 \quad f = \frac{v}{2\pi r} \quad ; \quad v \propto \frac{1}{n} \quad , \quad r \propto n^2$$

$$\Rightarrow f \propto \frac{1}{n^3}$$

$$\Rightarrow \frac{f_1}{f_2} = \frac{n_2^3}{n_1^3}$$

$$\Rightarrow \frac{1}{27} = \frac{n_2^3}{n_1^3}$$

$$\Rightarrow \frac{n_1}{n_2} = 3$$

$$Q57 \quad r \propto n^2$$

$$\Rightarrow \frac{r_n}{r_1} = \frac{n^2}{1^2}$$

$$\Rightarrow \frac{r_n}{a_0} = n^2$$

$$\Rightarrow r_n = n^2 a_0$$

$$Q58 \quad E_{2^{nd}} = -13.6 \frac{12}{2^2} \quad \therefore E_n^{th} = -13.6 \frac{Z^2}{n^2}$$

$$\Rightarrow E_{2^{nd}} = -3.4 \text{ eV}$$

$$\Rightarrow \text{Energy required} = 3.4 \text{ eV}$$

$$Q59 \quad r = \frac{60 n^2 h^2}{\pi m z c^2} \quad \text{for } K \text{ shell } n=1$$

$$\Rightarrow \frac{r_e}{r_u} = \frac{m_u}{m_e}$$

$$\Rightarrow r_u = \frac{m_e}{m_u} \times r_e \quad \leftarrow .53 \text{ \AA}$$

$$r_u = \frac{1}{207} \times .53 \text{ \AA} = 2.56 \times 10^{-3} \text{ \AA}$$

Q 60 → 10 different wavelengths means
the excitation was to $n=5$

$$\Rightarrow \frac{1}{\lambda} = R \left(1 - \frac{1}{5^2}\right)$$

$$\Rightarrow \boxed{\lambda = 95 \text{ nm}}$$

Q 61 → $E = +13.6 \left(1 - \frac{1}{25}\right) \text{ eV}$

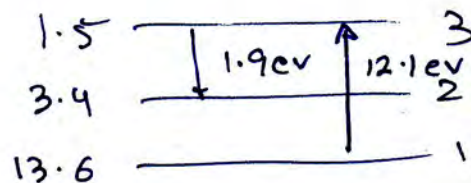
$$p = \frac{E}{c} = \frac{\left(13.6 \times \frac{24}{25} \times 1.6 \times 10^{-19}\right)}{3 \times 10^8} = 6.96 \times 10^{-27}$$

Same will be the momentum of hydrogen

$$\Rightarrow mv = 6.96 \times 10^{-27}$$

$$\Rightarrow v = \frac{6.96 \times 10^{-27}}{1.672 \times 10^{-27}} = 4.2 \text{ m/s}$$

Q 62



~~So Answer is 1.9 eV~~

So to emit 1st line of Balmer, the electron had to be excited to $n=3$

which requires 12.1 eV energy

Q 63 $f = \frac{v}{2\pi r}$ $v \propto \frac{1}{n}$, $r \propto n^2$

$$\Rightarrow f \propto \frac{1}{n^3}$$

$$\Rightarrow \frac{f_2}{f_1} = \frac{1^3}{2^3}$$

$$\Rightarrow \ln\left(\frac{f_2}{f_1}\right) = -3 \ln 2 \rightarrow x \quad \Rightarrow \boxed{y = -3x}$$

Q64 $\frac{1}{\lambda} = RZ^2 \left(\frac{1}{1^2} - \frac{1}{2^2} \right)$

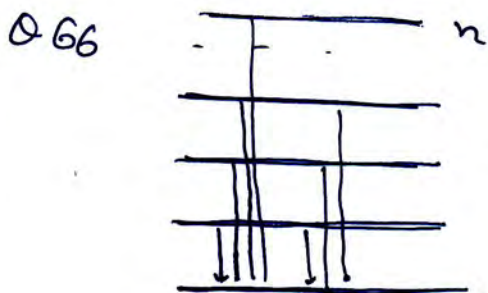
$\Rightarrow \lambda \propto \frac{1}{Z^2}$

So Least λ will be for doubly ionized Lithium

Q65 $T^2 \propto R^3$

$\frac{T_1^2}{T_2^2} = \frac{R^3}{(4R)^3}$

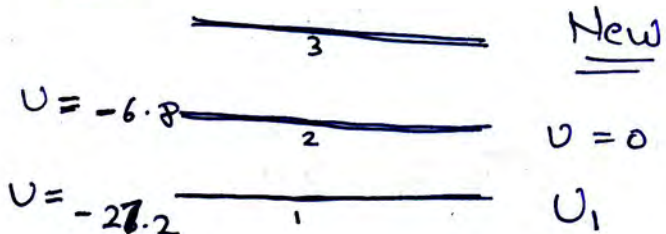
$\frac{T_1}{T_2} = \frac{1}{4}$



So if $n=2 \Rightarrow$ Lines = 1
 if $n=3 \rightarrow$ Lines = 3 = 1+2
 if $n=4 \rightarrow$ Lines = 6 = 1+2+3
 if $n=n \rightarrow$ Lines = 1+2+3+...+n-1

Q67

old



~~$\Rightarrow -27.2$~~

$-6.8 - (-27.2) = 0 - U_1$

$\Rightarrow U_1 = -20.4$

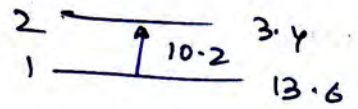
also $x_1 = 13.6$

$\Rightarrow E_1 = -20.4 + 13.6 = -6.8$

Now the differences remain the same even on changing reference

Q 68 The loss in KE = $\frac{K_0}{2}$

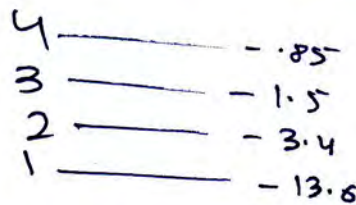
and a minimum loss of 10.2 eV is required to cause excitation



So Neutron should have 20.4 eV minimum to cause excitation

→ Any lesser amount of initial KE will cause inelastic collision

Q 69 $E = -K = \frac{U}{2}$



So as we go towards

ground state the total energy

becomes more Negative, hence it decreases

and from the formula we can see

$$\text{If } E \downarrow \Rightarrow U \downarrow \Rightarrow K \uparrow$$

Q 70

$$r \propto n^2$$

$$f \propto \frac{1}{n^3}$$

$$L \propto n$$

$$\Rightarrow frL \propto n^0$$

\Rightarrow constant for all orbits

Q 71

\because K_B represents a larger energy gap hence it has lower wavelength

$$\Rightarrow K_B \rightarrow p$$

$$K_A \rightarrow q$$

Q72 Energy difference is equal to the
 Energy of the $K\alpha$ photon = $\frac{hc}{\lambda} = \frac{1242 \text{ eV}\cdot\text{nm}}{.021}$
 $= \cancel{59 \text{ KeV}}$
 $= 59 \text{ KeV}$

Q73 $X^{200} \rightarrow A^{110} + B^{90}$
 increase in BE = mass defect energy = energy released
 $\Rightarrow \Delta BE = (110 \times 8.2 + 90 \times 8.2) - 7.4 \times 200$
 $= 160 \text{ MeV}$

Q74 Energy required = Loss in BE $C_{13} \rightarrow C_{12} + n$
 $= (BE)_{C_{13}} - (BE)_{C_{12}}$
 $= (13 \times 7.5) - (12 \times 7.68)$
 $= 5.34 \text{ MeV}$

Q75 $X \rightarrow BE = E_1$ $2X \rightarrow Y$
 $Y \rightarrow BE = E_2$
 Energy released = increase in BE
 $Q = E_2 - 2E_1$

Q76 $r = 0.53 \frac{n^2}{Z} \text{ \AA}$
 $Z \rightarrow 2$
 $= 1.06 \text{ \AA}$

Q77 $E = -3.4 \text{ eV} \Rightarrow n=2$
 $\Rightarrow L = \frac{nh}{2\pi} \Rightarrow \boxed{L = \frac{h}{\lambda}}$

Q 78

$$\begin{aligned} \text{no of fissions required per second} &= \frac{\text{Power required}}{\text{Energy released per fission}} \\ &= \frac{1 \text{ kW}}{200 \text{ MeV}} \\ &= \frac{1000}{200 \times 10^6 \times 1.6 \times 10^{-19}} \\ &= 3.125 \times 10^{13} \end{aligned}$$

Q 79

$$\begin{aligned} {}^2_1\text{H} &\rightarrow 1876 \text{ MeV} \\ n &\rightarrow 940 \text{ MeV} \\ p &\rightarrow 939 \text{ MeV} \end{aligned}$$

$$n + p = 1879 \text{ MeV}$$

∴ so for fission an extra 3 MeV is required which can be obtained by absorbing a γ photon of 3 MeV energy

~~Q 78~~

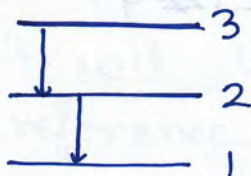
Exercise II

Q1: $hf = \phi + cv$

$\Rightarrow v = \left(\frac{h}{e}\right)f - \phi$

So v depends on $f \geq \phi \rightarrow$ emitter's properties

Q2



$$\frac{1}{\lambda_1} = R \left(\frac{1}{4} - \frac{1}{9} \right)$$

$$\Rightarrow \lambda_1 = \frac{36}{5R}$$

$$\frac{1}{\lambda_2} = R \left(1 - \frac{1}{4} \right)$$

$$\Rightarrow \lambda_2 = \frac{4}{3R}$$

$$x = \frac{\lambda_1}{\lambda_2} = \frac{\frac{36}{5R}}{\left(\frac{4}{3R}\right)} = \frac{27}{5}$$

$$y = \frac{p_1}{p_2} = \frac{h/\lambda_1}{h/\lambda_2} = \frac{\lambda_2}{\lambda_1} = \frac{5}{27}$$

$$z = \frac{E_1}{E_2} = \frac{hc/\lambda_1}{hc/\lambda_2} = \frac{\lambda_2}{\lambda_1} = \frac{5}{27}$$

$$\Rightarrow z = 1/x$$

Q3 $K = -E = 3.4 \text{ eV}$

$$\lambda = \frac{h}{p} = \frac{h}{\sqrt{2mK}}$$

$$\lambda = \frac{6.63 \times 10^{-34}}{\sqrt{2 \times 9.1 \times 10^{-31} \times 3.4 \times 1.6 \times 10^{-19}}}$$

$$= \frac{6.63 \times 10^{-34}}{\sqrt{2 \times 9.1 \times 10^{-31} \times 3.4 \times 1.6 \times 10^{-19}}}$$

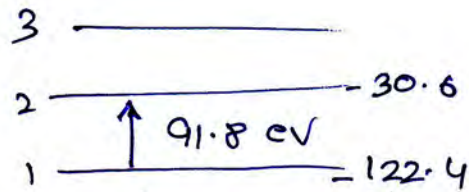
$$= 6.66 \times 10^{-10}$$

Q4

$$E = \frac{13.6 Z^2}{n^2}$$

$$\Rightarrow 122.4 = \frac{13.6 Z^2}{1^2}$$

$$\Rightarrow \boxed{Z=3}$$



→ To cause even a single jump an

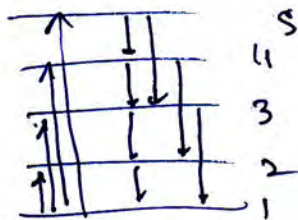
energy of 91.8 eV is required

So 90 eV is not sufficient

→ So ~~if~~ an electron of 91.8 eV KE can provide full of its KE to cause excitation & itself it can come to rest

→ if electron of KE 125 eV collides with an atom it can cause ionization with an ejected electron having energy $125 - 122.4 = 2.6$ eV

Q5 Ultraviolet light lies in the ~~Lyman~~ Lyman series and it can cause excitation from $n=1$ to higher orbits



but in de-excitation we can have a stepwise de-excitation which can release other wavelengths including ultraviolet and visible ~~to~~ & infrared red

Q5 \therefore Hydrogen is in ground state $\Rightarrow n=1$
 \Rightarrow the absorption can only be in Lyman series

Q7 Changing the reference does not affect the differences in energy of two levels
& since the energy of upper shells is higher
 \rightarrow it will be higher even with the new reference

@ ground state $U=0$, $K=13.6\text{ eV}$
 $\Rightarrow E=13.6\text{ eV}$

Q8 > if we consider motion of nucleus we have to consider reduced mass instead of mass of electron

$$\mu = \frac{m_N m_e}{m_N + m_e}$$

$$\Rightarrow \mu = \frac{m_e}{1 + \left(\frac{m_e}{m_N}\right)}$$

\Rightarrow the one with heavier nucleus will have higher reduced mass

$\therefore r \propto \frac{1}{\mu} \Rightarrow r_{\text{Hydrogen}} > r_{\text{Deuterium}}$

\therefore velocity is independent of mass, it does not matter

$\therefore E \propto m \Rightarrow$ Energy differences are more in deuterium \Rightarrow wavelengths would be lesser in case of deuterium

$\therefore L = \frac{nh}{2\pi} \Rightarrow$ 1st orbit $L = \frac{h}{2\pi}$ same for both

$$Q9 \quad r \propto n^2$$

$$A \propto r^2$$

$$\Rightarrow A \propto n^4$$

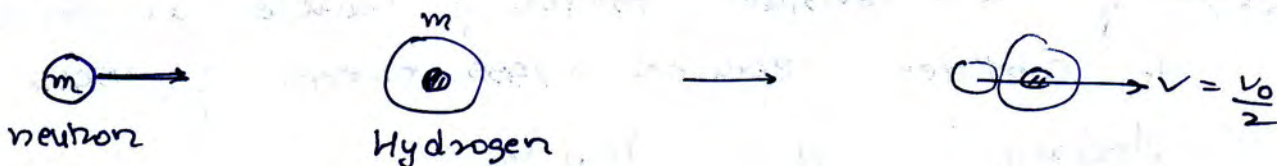
$$\Rightarrow \frac{A_n}{A_1} = \frac{n^4}{1^4}$$

$$\Rightarrow \left(\frac{A_n}{A_1} \right) = n^4$$

$$\Rightarrow \ln \left(\frac{A_n}{A_1} \right) = 4 \ln n$$

$$\Rightarrow \boxed{y = 4x}$$

Q10



$$\begin{aligned} \text{maximum possible loss in KE} &= \frac{1}{2} m v_0^2 - \frac{1}{2} 2m \left(\frac{v_0}{2} \right)^2 \\ &= \frac{1}{4} m v_0^2 \\ &= \frac{K_0}{2} \end{aligned}$$

$$\begin{aligned} \text{1st excitation energy of Hydrogen} &= 13.6 - 3.4 \\ &= 10.2 \end{aligned}$$

So the loss must at least be that much to cause excitation $\Rightarrow \frac{K_0}{2} \geq 10.2$
 $\Rightarrow K_0 \geq 20.4$

So if $K_0 < 20.4 \rightarrow$ No excitation \rightarrow elastic collision
 if $K_0 = 20.4 \rightarrow$ Total loss \rightarrow perfectly inelastic
 if $K_0 > 20.4 \rightarrow$ some loss \rightarrow inelastic

Q11 α decay \rightarrow loss of 2 protons, 2 neutrons
 $\rightarrow Z, A$ both decrease

β^- decay \rightarrow converts neutron to proton
 $\Rightarrow Z$ inc, $A \rightarrow$ same

β^+ decay \rightarrow converts proton to neutron
 $\Rightarrow Z$ dec, $A \rightarrow$ same

γ decay \rightarrow only energy
 $Z \rightarrow$ same, $A \rightarrow$ same

12 > $\lambda_{min} = \frac{hc}{eV} \Rightarrow \cancel{V} = \frac{hc}{e\lambda_{min}}$
 $\Rightarrow \cancel{V} = \frac{hc}{e\lambda}$
 $= \frac{6.63 \times 10^{-34} \times 3 \times 10^8}{1.6 \times 10^{-19} \times 66.3 \times 10^{-12}}$
 $= 18750 \text{ V}$
 $= 18.75 \text{ kV}$

λ de broglie = $\frac{h}{p}$
 $= \frac{h}{\cancel{(E/c)}} \frac{h}{\sqrt{2m(K.E)}} \rightarrow \text{eV}$
 $= \frac{6.63 \times 10^{-34}}{\sqrt{2 \times 9.1 \times 10^{-31} \times 1.6 \times 10^{-19} \times 18750}}$
 $= 8.97 \times 10^{-12} \text{ m} \approx 0.08 \text{ \AA}$

Q13: Since more energetic photons are emitted now
 \Rightarrow The total Energy increases \Rightarrow Intensity increases

also $\lambda_{\min} = \frac{hc}{eV} \Rightarrow V \uparrow \Rightarrow \lambda \downarrow$

Q14 initially nucleus has equal no of proton & neutrons
 \rightarrow in heavier elements no of neutrons is more
 \rightarrow neutron-proton ratio continuously increases



\rightarrow BE per nucleon increases & then decreases

Q15 $BE_{Ne} = (10m_p + 10m_n - M_1)c^2$
 $BE_{Ca} = (20m_p + 20m_n - M_2)c^2$



$\Rightarrow M_1 = 10(m_p + m_n) - \frac{BE_{Ne}}{c^2}$

$\Rightarrow M_1 < 10(m_p + m_n)$

also $M_2 - 2M_1 = \frac{1}{c^2} (2BE_{Ne} - BE_{Ca})$
 $= \frac{40}{c^2} \left(\left(\frac{BE}{A}\right)_{Ne} - \left(\frac{BE}{A}\right)_{Ca} \right)$
 $\rightarrow < 0$

$\Rightarrow M_2 - 2M_1 < 0$

$\Rightarrow M_2 < 2M_1$

Q16 A7 $\lambda = 0.173 \text{ years}$

decayed part $N_{\text{decayed}} = N_0 (1 - e^{-\lambda t})$

$.63 N_0 = N_0 (1 - e^{-\lambda t})$

$\Rightarrow e^{-\lambda t} = .37$

$\Rightarrow e^{-\lambda t} = 1/e$

$\Rightarrow -\lambda t = -1$

$\Rightarrow t = \frac{1}{\lambda} = \frac{1}{.173} \text{ years}$

B) half life = $\frac{.693}{\lambda} = \frac{0.693}{.173}$

C) $N = N_0 e^{-\lambda t}$

~~$\frac{3}{4} N_0 = N_0 e^{-\lambda t}$~~

$\Rightarrow N = N_0 e^{-(.173 \times 8)}$

~~$\Rightarrow \lambda t = \ln \frac{4}{3}$~~

$N = .25 N_0$

~~$\Rightarrow t = \frac{\ln \frac{4}{3}}{\lambda}$~~

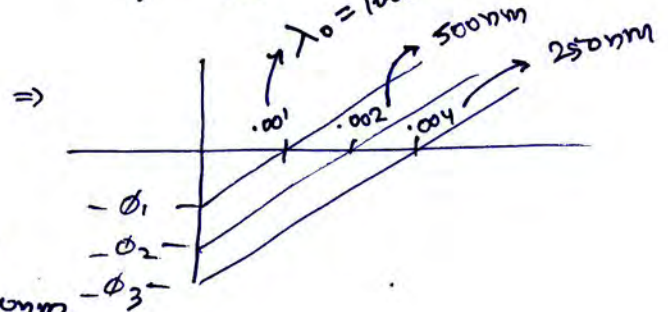
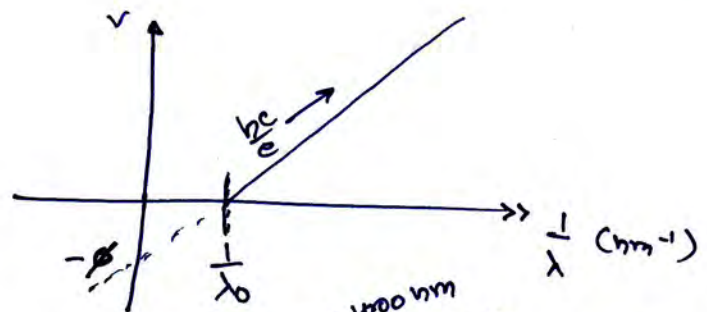
17 ~~$\frac{hc}{\lambda} = \frac{hc}{\lambda_0}$~~

$\frac{hc}{\lambda} = \phi + eV_s$

$\Rightarrow V_s = \frac{hc}{e\lambda} - \phi$

$\Rightarrow y = \left(\frac{hc}{e}\right) x - \phi$

$\Rightarrow \phi_1 : \phi_2 : \phi_3 = 1 : 2 : 4$



ultraviolet can eject from metal ① & ② $\because \lambda_{\text{ultraviolet}} < 400 \text{ nm}$

Exercise 3

Comprehension - 1

- 1> Since mass is not conserved, we cannot find the mass of that particle but still it is possible to find the total energy of that particle since total energy is conserved

$$\begin{aligned} E_{3rd \text{ particle}} &= E_{\text{neutron}} - E_{\text{proton}} - E_{\text{electron}} \\ &= (940.47) - (939.67 + 0.01) \\ &\quad - (0.51 + 0.39) \\ &= \cancel{0.37} \quad 0.39 \text{ MeV} \end{aligned}$$

→ This is the total energy but we cannot be sure how much of it is in the form of mass energy. hence "d"

- 2> "a" discussed in previous part

3>

$$\begin{array}{l} \text{TE} \\ \downarrow \\ \gamma \end{array} = \begin{array}{l} \text{KE} \\ \downarrow \\ \text{constant} = k \end{array} + \begin{array}{l} mc^2 \\ \downarrow \\ \text{constant} = m \end{array} \rightarrow \text{constant} = m$$

$$\Rightarrow \gamma = mc^2 + c \quad \text{hence "c"}$$

- 4> An isolated proton can never decay into a neutron since a neutron is heavier, hence it would be against energy conservation principles for such a reaction to occur, however if the proton possesses extra potential energy from its interactions with other particles in the nucleus, such a reaction would be feasible, in fact it does happen in nature.

Ex Comprehension 2

5> Q value = Total increase in the BE of system
= $BE_f - BE_i$
= $(E_2N_2 + E_3N_3) - E_1N_1$ "Magic 6"

6> The Nuclei with higher BE per nucleon also have a lower mass per nucleon.

⇒ ^{higher} ~~lower~~ BE per nucleon ⇒ lower mass per nucleon

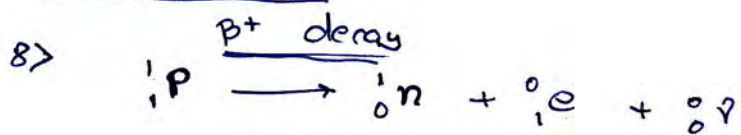
$$\Rightarrow \frac{M_{10}}{N_1} > \frac{M_1}{N_2} > \frac{M_2}{N_3}$$

7> Even though the BE per nucleon decreases for nuclei heavier than Z, but the total no of nucleons ~~is~~ also increases

$$TBE = \underbrace{(BE \text{ per Nucleon})}_{\text{decreasing}} \times \underbrace{(No \text{ of nucleons})}_{\text{increasing}}$$

hence it is observed that TBE increases but the relation of TBE vs Atomic mass No is not linear infact its slope decreases on increasing atomic mass implying that very heavy nuclei become increasingly instable since the TBE isnt increasing sufficiently.

Comprehension 3

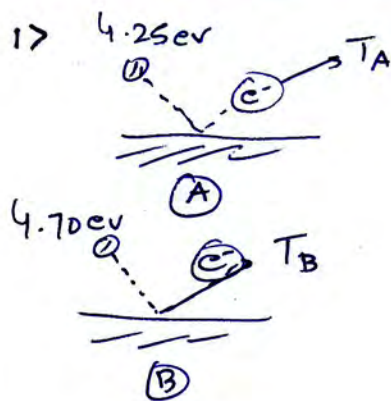


So answer is β

9) in β^- decay the atomic No rises by 1
 So two successive β^- decay \Rightarrow atomic No rises by 2
 hence answer is C

10) the net momentum has to be zero which is not possible in case of just one photon, hence answer is C

Match the columns



$$4.25 = \phi_A + T_A$$

$$4.70 = \phi_B + T_B$$

also $\lambda_B = 2\lambda_A$

$$\Rightarrow \frac{h}{p_1} = 2 \frac{h}{p_2}$$

$$\Rightarrow p_2 = 2p_1$$

$$\Rightarrow \sqrt{2mKE_1} = 2\sqrt{2mKE_2}$$

$$KE_1 = 4KE_2$$

$$T_A = 4T_B$$

$$T_A = 4(T_A - 1.5)$$

$$\Rightarrow \boxed{T_A = 2 \text{ eV}}$$

$$\Rightarrow \boxed{\phi_A = 2.25 \text{ eV}}$$

$$\boxed{T_B = 0.5 \text{ eV}}$$

$$\Rightarrow \boxed{\phi_B = 4.20 \text{ eV}}$$

$$27 \quad T^2 \propto r^3 \quad \text{and} \quad r \propto n^2$$

$$\Rightarrow T^2 \propto n^6$$

$$\Rightarrow T \propto n^3$$

$$\Rightarrow \frac{T_1}{T_2} = \frac{n_1^3}{n_2^3}$$

$$\Rightarrow \frac{\cancel{T_1}}{\cancel{8T_1}} = \frac{\cancel{n_1^3}}{\cancel{n_2^3}} \Rightarrow \frac{n_2^3}{n_1^3} = \frac{\cancel{8T_1}}{\cancel{T_1}}$$

$$\frac{8T_2}{T_2} = \frac{n_1^3}{n_2^3}$$

$$\Rightarrow \boxed{n_1 = 2n_2}$$

$\Rightarrow (n_1, n_2)$ can be $(4, 2)$ or $(6, 3)$

37 Theory Based

47 Theory Based

57 Theory Based

67 Theory Based

Exercise 4

$$Q17 \quad a) \quad \frac{hc}{\lambda} = \phi + eVs$$

$\lambda \rightarrow 4950 \text{ \AA}$ $\phi \rightarrow ?$ $eVs \rightarrow 0.6 \text{ V}$

$$\Rightarrow \phi = 1.9 \text{ eV}$$

$$b) \quad \frac{hc}{\lambda'} = \phi + eVs'$$

$\lambda' \rightarrow ?$ $\phi \rightarrow 1.9 \text{ eV}$ $eVs' \rightarrow 1.1 \text{ V}$

$$\Rightarrow \lambda' = 4125 \text{ \AA}$$

c) No change since magnetic field does not affect KE

$$Q2 \quad i) \quad P = \frac{dn}{dt} \times E_0 \rightarrow \text{Energy of each photon}$$

$\frac{dn}{dt} \rightarrow \text{No of photons emitted per second}$

$$\frac{dn}{dt} = \frac{(100 \text{ W})}{\frac{hc}{\lambda}} = 3 \times 10^{20} \text{ photons/sec}$$

$\frac{hc}{\lambda} \rightarrow 5890 \text{ \AA}$

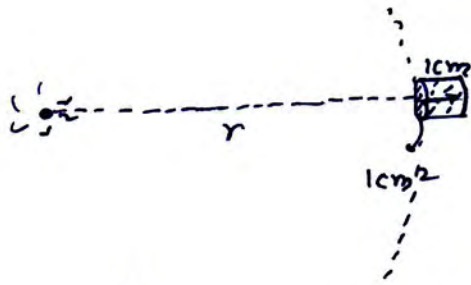
$$ii) \quad \text{Photon flux} = \frac{\left(\frac{dn}{dt}\right)}{4\pi r^2} = 1 \frac{\text{photon}}{\text{cm}^2 \text{ s}}$$

$$\frac{3 \times 10^{20}}{4\pi r^2} = 1$$

$$\Rightarrow r = 4.9 \times 10^4 \text{ km}$$



iii)



Photons intensity

$$\text{density of photon} = I \times \frac{1 \text{ cm}}{c} \rightarrow \text{speed of light}$$

$$= \frac{1 \text{ photon}}{\text{cm}^2 \cdot \text{sec}}$$

$$1 \text{ photon/cm}^3 = \frac{3 \times 10^{20}}{4\pi r^2} \times \frac{1 \text{ cm}}{300 \times 10^8 \text{ cm/s}}$$

$$\Rightarrow r = 282 \text{ m}$$

$$\text{iv)} \quad \text{photon flux} = \frac{3 \times 10^{20}}{4\pi \times (200)^2} = 5.96 \times 10^{14} \text{ photons/cm}^2$$

$$\begin{aligned} \text{photon density} &= \text{photon flux} \times \frac{1 \text{ cm}}{c} \\ &= 5.96 \times 10^{14} \times \frac{1}{300 \times 10^8} \\ &= 20 \times 10^3 \text{ photons/cm}^3 \end{aligned}$$

Q3

$$\Delta E = 13.6 Z^2 \left(1 - \frac{1}{2^2}\right) \text{ eV}$$
$$= 13.6 \times 3 \text{ eV}$$

So $\Delta E = \underbrace{\text{ionization Energy}}_{\text{Hydrogen}} + \text{KE}$

$$13.6 \times 3 = 13.6 + \text{KE}$$

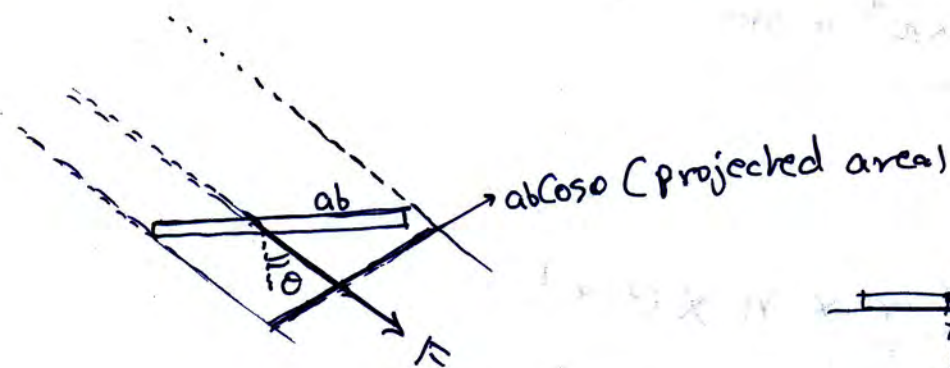
$$\text{KE} = 27.2 \text{ eV}$$

$$\Rightarrow \frac{1}{2} m v^2 = 27.2 \text{ eV}$$

$$\Rightarrow \frac{1}{2} \times 9.1 \times 10^{-31} = 27.2 \times 1.6 \times 10^{-19}$$

$$\Rightarrow \boxed{v = 3.1 \times 10^6 \text{ m/s}}$$

Q4



$$\text{force} = \frac{I}{c} \times \text{projected area}$$
$$= \frac{I}{c} \times ab \cos \theta$$

$$a = \frac{F \sin \theta - 4N}{m}$$

$$N = mg + F \cos \theta$$

$$Q5: \quad \frac{3}{2} kT = \frac{1}{2} m v^2$$

$$\Rightarrow 3kT = \frac{(mv)^2}{m}$$

$$\Rightarrow p = \sqrt{3mkT}$$

$$\Rightarrow \lambda = \frac{h}{p} = \frac{h}{\sqrt{3mkT}}$$

$$h = 6.625 \times 10^{-34} \text{ J}\cdot\text{s}$$

$$m = 1.66 \times 10^{-27} \text{ kg}$$

$$k = 1.38 \times 10^{-23} \text{ J/K}$$

$$T = 400 \text{ K}$$

$$Q6: \quad T_{1/2} = 5568 \text{ years}$$

$$A = A_0 e^{-\lambda t}$$

$$\frac{A}{A_0} = e^{-\lambda t}$$

$$\Rightarrow \frac{3.9}{15.6} = e^{-\frac{\ln 2}{T_{1/2}} t}$$

$$\Rightarrow t = 1.118 \times 10^4 \text{ years}$$

$$Q7 \quad V = \frac{kQ}{r}$$

$$V = \frac{k}{r} (r \times \eta \times e \times t)$$

\downarrow rate \downarrow efficiency

$$2 = \frac{9 \times 10^9}{10^{-2}} (5 \times 10^{10} \times .4 \times 1.6 \times 10^{-19} \times t)$$

$$\Rightarrow t = 6.9 \times 10^{-4} \text{ sec}$$

Q8 $\sqrt{f} = a(z-b)$

$\Rightarrow \sqrt{\frac{c}{\lambda}} = a(z-b)$

$\Rightarrow \sqrt{\frac{\lambda_{AL}}{\lambda_{zn}}} = \frac{(z_{zn}-b)}{(z_{AL}-b)}$

Annotations: $\lambda_{AL} \rightarrow 887$, $\lambda_{zn} \rightarrow 146$, $z_{zn} \rightarrow 30$, $z_{AL} \rightarrow 13$

$\Rightarrow \boxed{b = 1.4}$

$\sqrt{\frac{\lambda_{Fe}}{\lambda_{AL}}} = \frac{(z_{AL}-b)}{(z_{Fe}-b)}$

Annotations: $\lambda_{AL} \rightarrow 887$, $z_{AL} \rightarrow 13$, $z_{Fe} \rightarrow 26$, $b \rightarrow 1.4$

$\Rightarrow \lambda_{Fe} = 198 \text{ pm}$

Q9

$\sqrt{f} = a(z-b)$

Annotations: $\sqrt{f} \rightarrow 4.2 \times 10^{18}$, $a \rightarrow \sqrt{\frac{3RC}{4}}$, $b \rightarrow 1$

$R = 1.1 \times 10^7$

$C = 3 \times 10^8$

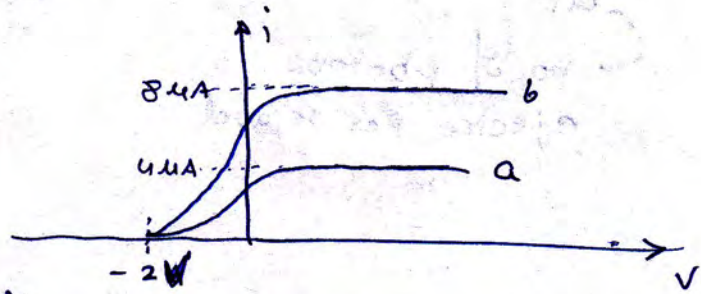
$\Rightarrow z = 42$

Exercise ~~IV~~ 5

1) $E = \phi + KE_{max}$

$\Rightarrow 5\text{eV} = 3\text{eV} + eV_s$

$\Rightarrow \boxed{V_s = 2\text{V}}$



and on doubling intensity
the saturation current
also doubles

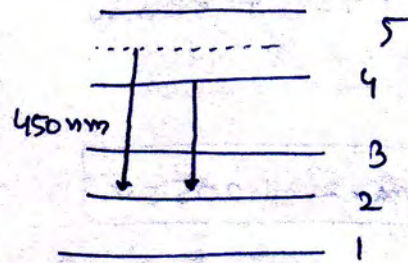
2) $\frac{1}{\lambda} = RZ^2 \left(\frac{1}{m^2} - \frac{1}{n^2} \right)$

$\frac{1}{450 \times 10^{-9}} = 1.09 \times 10^7 \times 12 \left(\frac{1}{2^2} - \frac{1}{n^2} \right)$

$\Rightarrow \boxed{n = 4.65}$

So exact 450 nm will be emitted
from a transition from 4.65 \rightarrow 2 quantum no.
(which is not possible)

So the closest wavelength
to 450 nm & between
(450 & 700) will be
from 4 \rightarrow 2 quantum jump



ie ~~$\frac{1}{\lambda}$~~ $E = 13.6 \left(\frac{1}{2^2} - \frac{1}{16} \right)$

$\boxed{E = 2.55\text{eV}}$

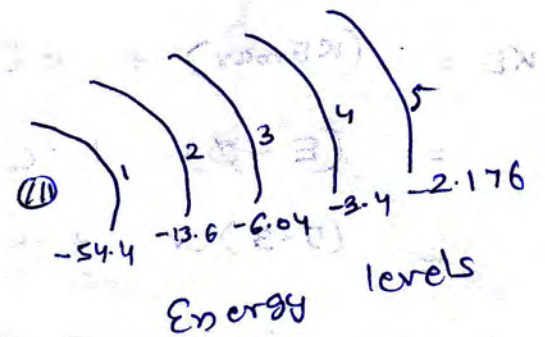
$\Rightarrow E = \phi + KE_{max}$

$\Rightarrow 2.55 = 2 + KE_{max}$

$\Rightarrow \boxed{KE_{max} = 0.55\text{eV}}$

So now photons will be emitted due to deexcitation

between 2ev & 4ev will be due to



$$5 \rightarrow 3 : = 6.04 - 2.176 = \boxed{3.864 \text{ eV}}$$

$$4 \rightarrow 3 : = 6.04 - 3.4 = \boxed{2.64 \text{ eV}}$$

Q5 $n = 10^{16}$ photons per metre square per second

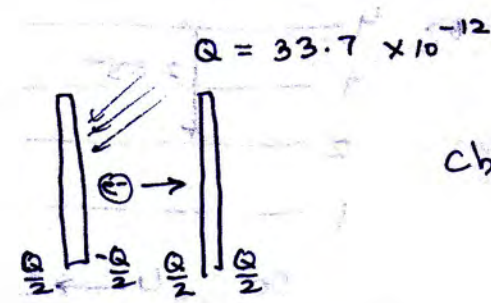
$\Rightarrow n \times A$ photons per second

\Rightarrow no of electrons ejected = $nA \times \alpha$ per sec
where $\alpha = \frac{1}{10^6}$

\Rightarrow no of electrons ejected in 10 sec = $nA \alpha \times 10$

$$N_0 = 10^{16} \times 5 \times 10^{-4} \times \frac{1}{10^6} \times 10$$

$$\boxed{N_0 = 5 \times 10^7}$$



charge on the left side of right plate

$$q = \frac{Q}{2} \times N_0 \times e$$

$$= \frac{33.7 \times 10^{-12}}{2} \times 5 \times 10^7 \times 1.6 \times 10^{-19}$$

$$= 8.85 \times 10^{-12} \text{ C}$$

$$\Rightarrow E = \frac{(q/A)}{\epsilon_0} = \frac{(8.85 \times 10^{-12})}{(5 \times 10^{-4})} = \boxed{2000 \text{ N/C}}$$

$$\begin{aligned}
 KE &= (KE_{\max}) + e(Ed) \\
 &= (E - \phi) + e(2000 \times 10^{-2}) \\
 &= (5 - 3) \text{ eV} + e(20 \text{ V}) \\
 &= 3 \text{ eV} + 20 \text{ eV} \\
 &= 23 \text{ eV}
 \end{aligned}$$

67 $E = -KE = \frac{U}{2}$

$\Rightarrow KE = -E$

$\Rightarrow KE = -(3.4)$
 $= 3.4 \text{ eV}$

$\lambda_{\text{de Broglie}} = \frac{h}{p}$

$= \frac{h}{\sqrt{2m \cdot KE}}$

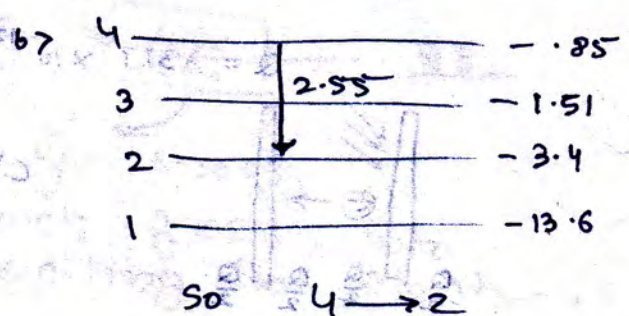
~~$= \frac{h}{mv}$~~

$= \frac{6.63 \times 10^{-34}}{\dots}$

$\sqrt{2 \times (9.1 \times 10^{-31}) \times 3.4 \times 1.6 \times 10^{-19}}$

$= 0.66 \times 10^{-9}$

77 a) $E = \phi + KE_{\max}$
 $= 1.82 + 0.73$
 $= 2.55 \text{ eV}$



c) $L_i = 4 \left(\frac{h}{2\pi} \right)$
 $L_f = 2 \left(\frac{h}{2\pi} \right)$

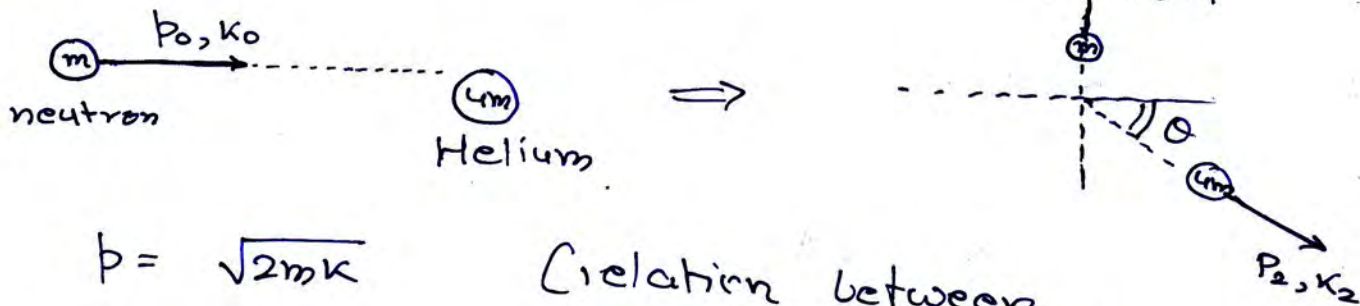
$|\Delta L| = \frac{2 \cdot h}{2\pi} = \frac{h}{\pi}$

d) $p_{\text{photon}} = p_{\text{hydrogen atom}}$

$\frac{E}{c} = mv$

$v = \frac{E}{mc} = \frac{2.55 \times (10^{-19} \times 1.6)}{(1.672 \times 10^{-27}) \times (3 \times 10^8)}$

Q8



$p = \sqrt{2mk}$ (relation between momentum & KE)

Conservation of momentum

x

$$p_0 = p_2 \cos \theta$$

$$\Rightarrow \sqrt{2mk_0} = \sqrt{2(4m)k_2} \cos \theta$$

$$\Rightarrow \boxed{k_0 = 4k_2 \cos^2 \theta} \quad \text{--- (i)}$$

y

$$p_1 = p_2 \sin \theta$$

$$\Rightarrow \sqrt{2mk_1} = \sqrt{2(4m)k_2} \sin \theta$$

$$\Rightarrow \boxed{k_1 = 4k_2 \sin^2 \theta} \quad \text{--- (ii)}$$

$$\text{(i)} + \text{(ii)} \Rightarrow \boxed{k_0 + k_1 = 4k_2} \quad \text{--- (I)}$$

also

$$\boxed{k_0 = k_1 + k_2 + \Delta E} \quad \text{--- (II)}$$

Loss of Energy (which goes into exciting the electron)

Solving I & II

$$k_1 = \frac{3k_0}{5} - \frac{4}{5} \Delta E$$

$$\Delta E = 13.6 \times 2^2 \left(1 - \frac{1}{n^2}\right)$$

$$k_2 = \frac{3k_0}{2} - \frac{\Delta E}{5}$$

for $n=1$ (ie No excitation)

$$k_1 = 39, \quad k_2 = 26$$

for $n=2$

$$k_1 = 6.36, \quad k_2 = 17.84$$

for $n=3$

$$k_1 = 0.312, \quad k_2 = 16.328$$

for $n=4$

$$k_1 = -ve \rightarrow \text{Not possible}$$

So at max the electron will be excited to $n=3$

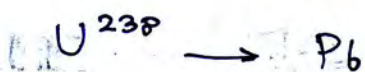
$$\text{So } h\nu = 13.6 \times 2^2 \left(\frac{1}{n^2} - \frac{1}{m^2} \right) \text{ eV}$$

$$\text{for } n=2, m=3 \quad \therefore \nu = 1.82 \times 10^{15}$$

$$\text{for } n=1, m=3 \quad \therefore \nu = 11.67 \times 10^{15}$$

$$n=1, m=2 \quad \therefore \nu = 9.84 \times 10^{15}$$

$$9) \quad T_{\frac{1}{2}} = 4.5 \times 10^9 = \frac{\ln 2}{\lambda}$$



$$U^{238} \quad \text{No:} = \text{No} e^{-\lambda t}$$

$$Pb \quad \text{No:} = \text{No} (1 - e^{-\lambda t})$$

$$\Rightarrow \frac{\text{No: Pb}}{\text{No: } U^{238}} = \frac{(1 - e^{-\lambda t})}{e^{-\lambda t}} = \frac{1 - e^{-\frac{\ln 2}{4.5 \times 10^9} \times 1.5 \times 10^9}}{e^{-\frac{\ln 2}{4.5 \times 10^9} \times 1.5 \times 10^9}}$$

$$= \frac{1 - 2^{-1/3}}{2^{-1/3}} = \frac{1 - \frac{1}{1.26}}{\frac{1}{1.26}} = \frac{1 - e^{-\frac{\ln 2}{3}}}{e^{-\frac{\ln 2}{3}}}$$

$$= 0.26$$

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$$KE = 0.327 \text{ eV}$$

$$T_{1/2} = 700 \text{ sec}$$

$$\frac{1}{2} mv^2 = 0.327 \times 1.6 \times 10^{-19} \text{ J}$$

$$\frac{1}{2} \times 1.675 \times 10^{-27} \frac{v^2}{\text{J}} = 0.327 \times 1.6 \times 10^{-19}$$

$$\Rightarrow v = 0.25 \times 10^4$$

$$t = \frac{\text{dist}}{\text{velocity}} = \frac{10}{0.25 \times 10^4} = 4 \times 10^{-3} \text{ s}$$

$$\begin{aligned} \text{fraction of Neutrons decayed} &= 1 - e^{-\lambda t} \\ &= 1 - e^{-\frac{0.693}{700} \times 4 \times 10^{-3}} \\ &= 3.96 \times 10^{-6} \end{aligned}$$

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$$\sqrt{f} = a(z-b)^2$$

$$4.2 \times 10^{18} \quad \rightarrow \quad \sqrt{\frac{3RC}{4}} \quad ; \quad R = 1.1 \times 10^7 \text{ m}^{-1}$$

$$C = 3 \times 10^8 \text{ m/s}$$

$$\Rightarrow z = 42$$

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$$r = R_0 A^{1/3}$$

$$\Rightarrow \frac{r}{r_{\text{He}}} = \left(\frac{A}{A_{\text{He}}} \right)^{1/3}$$

$$(14)^{1/3} = \left(\frac{z+30}{4} \right)^{1/3}$$

$$\Rightarrow \boxed{z = 26}$$

$$f = a(z-b)^2$$

$$f = \frac{3RC}{4} (26-1)^2$$

$$R = 1.1 \times 10^7$$

$$C = 3 \times 10^8$$

$$\Rightarrow \boxed{f = 1.546 \times 10^{18} \text{ Hz}}$$